

# Design of Maximum Torque Per Ampere Control Method In Squirrel Cage Three-Phase Induction Motor

Regina Chelinia Erianda Putri<sup>1\*</sup>, Feri Yusivar<sup>2</sup>

<sup>1</sup>*Faculty of Science and Technology, Sanata Dharma University,  
Yogyakarta, 55281, Indonesia*

<sup>2</sup>*Faculty of Engineering, University of Indonesia, Depok, 16424, Indonesia*

*\*Corresponding Author: regina.chelinia@usd.ac.id*

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## Abstract

Improving the performance of three-phase induction motors is currently carried out by various control methods. One of them is controlling a three-phase induction motor using the Maximum Torque Per Ampere (MTPA) method. This paper focuses on the study of modeling specific motor models using the MTPA method. The purpose of the study is to prove that with the squirrel cage motor model, the speed can be increased above its rating. The MTPA method is a method of controlling a three-phase induction motor by controlling the current from the torque speed. Modeling is tested to see the responsiveness of the modeled system. The experimental results were tested using two-speed references and the system showed that MTPA control induction motors can improve the performance of three-phase induction motors. The results from the design show that the MTPA method can increase the performance of three-phase induction motors to reach 84.4%. The results of this study can be used as one way to model induction motors.

**Keywords:** Induction Motor, Modelling, MTPA

## 1 Introduction

Developments in the field of transportation in the current era are growing rapidly. However, it is not balanced with waste treatment, making the environment polluted with smoke pollution. According to the results of the study "In the last 100 years the earth has increased in temperature up to 0.18 degrees Celsius" [1].

The transition from fossil fuel energy to electrical energy as energy in the field of transportation requires one component of electric vehicle design, namely the induction motor. Induction motor is the leading technology in many industrial applications, nevertheless, suitable IM designs are proposed even for automotive applications[2]. A



three-phase induction motor is an electronic device that aims to convert electrical energy into mechanical energy. A widely used induction motor is a three-phase induction motor known as an asynchronous motor, called because of the difference in speed from the rotation of the rotor to the rotation speed of the stator.

There are several ways to improve motor capabilities above the rate discussed in previous studies. MTPA Method has several various developments such as the title Direct Quadrature (D-Q) Modeling in the Speed Control System of Three Phase Induction Motors With Field Oriented Control (FOC) Based on P-I Controlled [3] study discusses controlling induction motors with FOC based on PI controllers. Speed Sensorless Control of Parallel Connected Dual Induction Motor Fed by Single Inverter using Direct Torque Control [4] discusses controlling two induction motors with parallel induction motors. Another research titled Comparative Performance of Induction Motor Speed Controller System with Flux Weakening Control discusses the purpose of controlling  $i_q^*$  by limiting where there is  $|i_q|$  input [5].

The purpose of this study is to prove that with certain motor models, speed can be increased above its rating. The MTPA method is a three-phase induction motor control method by adjusting the reference input of torque current and flux current to control the rotational speed of the induction motor. Recently, the maximum torque per ampere (T/A) scheme has been proposed to minimize the stator current and reduce inverter losses [6]. Neither “minimum loss” nor “maximum torque per ampere” provided optimal motor drive performance and that drive performance was optimal between the two conditions [7]. MTPA is designed to ensure that the current used is the minimum  $i_d$  current for development at motor torque, with the total stator flux controlled by the MTPA criterion.

## 2 Research Method

The system uses models and methods, namely induction motor models, Clark-Park transformation methods, Rotor Field Oriented Control (RFOC), and MTPA modeling.

### A. Induction motor model

Induction motor modeling uses the stator voltage vector  $(v_s)'$ , the stator current vector  $(i_s)'$ , the stator flux vector  $(\psi_s)'$  and the rotor flux vector  $(\psi_r)'$ . The general equation of the induction motor is as follows.

$$\vec{V}_s' = R_s \vec{i}_s' + \frac{d}{dt} \vec{\psi}_s' + j\omega_e \vec{\psi}_s' \quad (\text{Eq. 1})$$

$$\vec{V}_r' = R_r \vec{i}_r' + \frac{d}{dt} \vec{\psi}_r' + j(\omega_e - \omega_r) \vec{\psi}_r' \quad (\text{Eq. 2})$$

$$\vec{\psi}_s' = L_s \vec{i}_s' + L_m \vec{i}_r' \quad (\text{Eq. 3})$$

$$\vec{\psi}_r' = L_r \vec{i}_r' + L_m \vec{i}_s' \quad (\text{Eq. 4})$$

### B. Clark-Park Transformation

The induction motor used is a three-phase induction motor, but modeling is carried out in two phases which aims to simplify calculations and analysis. Transformation from three phases to two phases, the transformations used are Clarke Transformation and Park Transformation. [8]

The Clarke transform is a transformation that transforms a system that is on the  $(abc)$  axis into a stationary state frame of reference  $(\alpha\beta)$  axis). In the stator frame of reference,  $\omega_e = 0$  and then in the cage rotor type, the terminals are briefly connected so that the rotor voltage is  $V_r = 0$ . The substitution of the equation of stator current and rotor current obtained induction motor model in the  $\alpha\beta$  axis becomes,

$$\frac{d}{dt} i_{s\alpha} = \left( -\frac{R_s}{\sigma L_s} - \frac{(1-\sigma)}{\sigma \tau_r} \right) i_{s\alpha} + \frac{L_m}{\sigma L_s L_r \tau_r} \psi_{r\alpha} + \frac{L_m \omega_r}{\sigma L_s L_r} \psi_{r\beta} + \frac{1}{\sigma L_s} V_{s\alpha} \quad (\text{Eq. 5})$$

$$\frac{d}{dt} i_{s\beta} = \left( -\frac{R_s}{\sigma L_s} - \frac{(1-\sigma)}{\sigma \tau_r} \right) i_{s\beta} - \frac{L_m \omega_r}{\sigma L_s L_r} \psi_{r\alpha} + \frac{L_m}{\sigma L_s \tau_r L_r} \psi_{r\beta} + \frac{1}{\sigma L_s} V_{s\beta} \quad (\text{Eq. 6})$$

$$\frac{d}{dt} \psi_{r\alpha} = \frac{R_r}{L_r} L_m i_{s\alpha} - \frac{R_r}{L_r} \psi_{r\alpha} - \omega_r \psi_{r\beta} \quad (\text{Eq. 7})$$

$$\frac{d}{dt} \psi_{r\beta} = \frac{R_r}{L_r} L_m i_{s\beta} + \omega_r \psi_{r\alpha} - \frac{R_r}{L_r} \psi_{r\beta} \quad (\text{Eq. 8})$$

with  $\sigma = \frac{L_s L_r - L_m^2}{L_s L_r}$  and  $\tau_r = \frac{L_r}{R_r}$

Park transform is a transformation that transforms a two-phase system that is on a stationary frame of reference  $(\alpha\beta)$  axis) transformed in a rotating frame of reference  $(dq)$  axis). In the rotor frame of reference the location  $\omega_e$  is put together by the axis of the rotor

causing the magnitude of  $\omega_e$  is not equal to zero. The stator voltage transformation in equations (1)-(4) will be [9]:

$$\frac{d}{dt} i_{sd} = \left( -\frac{R_s}{\sigma L_s} - \frac{L_m^2}{\sigma L_s L_r \tau_r} \right) i_{sd} + \omega_e i_{sq} + \frac{L_m}{\sigma L_s L_r \tau_r} \psi_{rd} + \frac{L_m}{\sigma L_s L_r} \omega_r \psi_{rq} + \frac{1}{\sigma L_s} V_{sd} \quad (\text{Eq. 9})$$

$$\frac{d}{dt} i_{sq} = -\omega_e i_{sd} + \left( -\frac{R_s}{\sigma L_s} - \frac{L_m^2}{\sigma L_s L_r \tau_r} \right) i_{sq} - \frac{L_m}{\sigma L_s L_r} \omega_r \psi_{rd} + \frac{L_m}{\sigma L_s L_r \tau_r} \psi_{rq} + \frac{1}{\sigma L_s} V_{sq} \quad (\text{Eq. 10})$$

$$\frac{d}{dt} \psi_{rd} = \frac{R_r}{L_r} L_m i_{sd} - \frac{R_r}{L_r} \psi_{rd} + (\omega_e - \omega_r) \psi_{rq} \quad (\text{Eq. 11})$$

$$\frac{d}{dt} \psi_{rq} = \frac{R_r}{L_r} L_m i_{sq} - (\omega_e - \omega_r) \psi_{rd} - \frac{R_r}{L_r} \psi_{rq} \quad (\text{Eq. 12})$$

with,  $\sigma = \frac{L_s L_r - L_m^2}{L_s L_r}$  and  $\tau_r = \frac{L_r}{R_r}$  and rotor speed equation  $\frac{d}{dt} \omega_r = \frac{T_e - T_l}{J}$ :

While the mechanical equation of a motor that has a polar p-tide. In this case, electromagnetic torque  $T_e$  expressed by,

$$T_e = p \left( \frac{L_m}{L_r} \right) (i_{s\beta} \psi_{r\alpha} - i_{s\alpha} \psi_{r\beta}) \quad (\text{Eq. 13})$$

$$T_e = p \left( \frac{L_m}{L_r} \right) (i_{sq} \psi_{rd} - i_{sd} \psi_{rq}) \quad (\text{Eq. 14})$$

The parameters used are as follows:

$R_r$ = Resistance on the rotor ( $\Omega$ )	$V_{s\alpha}$ = Stator voltage on $\alpha$ axis (V)
$R_s$ = Resistance on the stator ( $\Omega$ )	$V_{s\beta}$ = Stator voltage on the $\beta$ axis (V)
$L_m$ = Magnetic inductance (H)	$V_{sd}$ = Stator voltage on the d-axis (V)
$L_s$ = Magnetic inductance (H)	$V_{sq}$ = Stator voltage on the q-axis (V)
$L_r$ = Magnetic inductance (H)	$\psi_{r\alpha}$ = Flux of $\alpha$ -axis rotor (Wb)
$\sigma$ = Leakage Coefficient	$\psi_{r\beta}$ = Flux of $\beta$ -axis rotor (Wb)
$i_{s\alpha}$ = $\alpha$ axis stator current (A)	$\psi_{rd}$ = d-axis rotor flux (Wb)
$i_{s\beta}$ = $\beta$ axis stator current (A)	$\psi_{rq}$ = q-axis rotor flux (Wb)
$i_{sd}$ = d-axis stator current (A)	$\omega_r$ = Rotor velocity (rad/s)
$i_{sq}$ = stator current q axis (A)	$\omega_e$ = Rotating field speed (rad/s)
$T_e$ = Electromagnetic torque (Nm)	$p$ = number of poles or poles
$T_l$ = Load torque (Nm)	$\tau_r$ = Rotor constant time

### C. Rotor Field Oriented Control (RFOC)

The orientation of the FOC (Field Oriented Control) control used has three frames of reference, named the rotor-stator and the air gap. RFOC not require additional processes to separate the interrelationships of variables in the equation. Rotor-oriented FOC (RFOC) can separate (decoupling) flux and torque components so that they can be controlled by d-axis stator current ( $i_{sd}$ ) and q-axis stator current ( $i_{sq}$ ) respectively. The separation of the two components  $U_{sd}$  and  $U_{sq}$  is a linear part of the stator voltage after the decoupling process [10].  $V_{cd}$  and  $V_{cq}$  are the non-linear part of the stator voltage after the decoupling process is carried out, as follows,

$$U_{sd} = R_s i_{sd} + L_s \sigma \frac{d}{dt} i_{sd} \quad (\text{Eq. 15})$$

$$U_{sq} = R_s i_{sq} + L_s \sigma \frac{d}{dt} i_{sq} \quad (\text{Eq. 16})$$

$$V_{cd} = -\sigma L_s \omega_e i_{sq} + \frac{L_m}{L_r} \frac{d}{dt} \psi_{rd} \quad (\text{Eq. 17})$$

$$V_{cq} = \sigma L_s \omega_e i_{sd} + \frac{L_m}{L_r} \omega_e \psi_{rd} \quad (\text{Eq. 18})$$

Then the current controller model is modeled as follows:

$$v_{sd}^* = -k_{idp} i_{sd} + k_{idp} i_{sd}^* + k_{idi} x_{sd} - \sigma L_s N \omega_m i_{sq1}^* - \sigma L_s \frac{R_r i_{sq1}^{*2}}{L_r i_{sd2}^*} \quad (\text{Eq. 19})$$

$$v_{sq}^* = -k_{iqp} i_{sq} + k_{iqp} i_{sq}^* + k_{iqi} x_{sq} + \sigma L_s N \omega_m i_{sd1}^* + \sigma L_s \frac{R_r i_{sd1}^* i_{sq1}^{*2}}{L_r i_{sd2}^*} + (1 - \sigma) L_s N \omega_m i_{sd2}^* + \frac{(1 - \sigma) L_s R_r}{L_r} i_{sq1}^* \quad (\text{Eq. 20})$$

$$\text{Where } k_{idp} = \frac{\sigma L_s}{T_d}, k_{idi} = \frac{R_s}{T_d}, k_{iqp} = \frac{\sigma L_s}{T_d}, k_{iqi} = \frac{R_s}{T_d}$$

Further, the first order of the reference current of the slip frequency and decoupling calculation becomes,

$$\frac{d}{dt} i_{sd1}^* = \frac{1}{T_d} i_{sd}^* - \frac{1}{T_d} i_{sd1}^* \quad (\text{Eq. 21})$$

$$\frac{d}{dt} i_{sq1}^* = \frac{1}{T_d} i_{sq}^* - \frac{1}{T_d} i_{sq1}^* \quad (\text{Eq. 22})$$

$$\frac{d}{dt} i_{sd2}^* = \frac{1}{T_2} i_{sd}^* - \frac{1}{T_2} i_{sd2}^* \quad (\text{Eq. 23})$$

### D. MTPA Modelling

In fact, for designs produced with high-speed motors, increasing the current ratio limit allows achieving the same rated efficiency but with a lower slot area. This condition is suitable for inverter driven systems and optimized with the Maximum Torque per Ampere method. The maximum torque per ampere condition occurs when a certain torque

speed condition is achieved at the minimum stator current [11]. Normal rate speed electric motor will occur if the motor parameters from the real parameter. The process of the Maximum Torque Per Ampere Method in the MTPA condition process identified for a particular motor torque, the stator current components used are  $i_d$  and  $i_q$ . MTPA is operated under the condition of each  $d$  and  $q$  axis flux component in a synchronous reference frame using equations [12][13]. Flow-related signals are used to obtain information about the magnitude of the current that controls the flow. The energy stored in the magnetizing inductance remains constant.

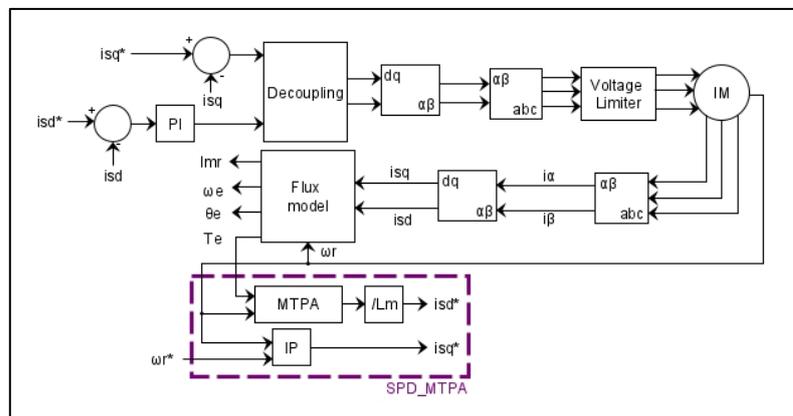
The Maximum Torque Per Ampere method is shown in Fig. 1. The system is tested using Matlab – Simulink – Cmx. The component values of the  $d$  and  $q$  axes for the flux synchronous reference frame for the MTPA method are given by the equation.

$$\psi_{ds}|_{MTPA} = \frac{L_s}{L_m} \sqrt{\frac{2T_e L_r}{P}} \tag{Eq. 24}$$

$$\psi_{qs}|_{MTPA} = \frac{\sigma L_s}{L_m} \sqrt{\frac{2T_e L_r}{P}} \tag{Eq. 25}$$

The values of the total flux components on the  $d$  and  $q$  axes in the synchronous reference frame are shown as

$$|\vec{\psi}_s|_{MTPA} = \frac{L_s}{L_m} \sqrt{\frac{2L_r (1 + \sigma^2) T_e}{P}} \tag{Eq. 26}$$



**Figure 1 . Block Process Diagram MTPA Method**

Then substitute  $\omega_{sl} = \frac{R_r i_{sq1}^*}{L_r i_{sd2}^*}$ ,  $v_{sd} = v_{sd}^*$ , and  $v_{sq} = v_{sq}^*$ ,  $|\psi_s| = \frac{L_s}{L_m} \sqrt{\frac{2L_r(1+\sigma^2)i_{sq}^*}{P}}$  so

$$i_{sd}^* = 1 + \frac{L_s}{L_m^2} \sqrt{\frac{2L_r(1+\sigma^2)i_{sq}^*}{P}}$$

The modeling results that have been linearized into,

$$\begin{aligned} \frac{d}{dt} \Delta i_{sd} = & \left( -\frac{k_{idp} + R_s}{\sigma L_s} - \frac{R_r(1-\sigma)}{\sigma L_r} \right) \Delta i_{sd} + \left( N\omega_{m0} + \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta i_{sq} + \left( \frac{L_m R_r}{\sigma L_s L_r^2} \right) \Delta \psi_{rd} + \left( \frac{NL_m \omega_{m0}}{\sigma L_s L_r} \right) \Delta \psi_{rq} + \\ & \left( \frac{k_{idi}}{\sigma L_s} \right) \Delta x_{sd} + \left( \frac{R_r i_{sq0}^*}{L_r i_{sd20}^*} - \frac{2R_r i_{sq10}^*}{L_r i_{sd20}^*} - N\omega_{m0} \right) \Delta i_{sq1}^* + \left( -\frac{R_r i_{sq0}^* i_{sq10}^*}{L_r i_{sd20}^{*2}} + \frac{R_r i_{sq10}^{*2}}{L_r i_{sd20}^{*2}} \right) \Delta i_{sd2}^* + \\ & \left( \frac{1}{2} \frac{k_{idp}}{\sigma L_m^2} \left( \frac{2L_r(1+\sigma^2)i_{sq0}^*}{P} \right)^{-\frac{1}{2}} \right) \Delta i_{sq}^* + \left( N i_{sq0}^* + \frac{NL_m \psi_{rq0}}{\sigma L_s L_r} - N i_{sq10}^* \right) \Delta \omega_m \quad (Eq. 27) \end{aligned}$$

$$\begin{aligned} \frac{d}{dt} \Delta i_{sq} = & \left( -N\omega_{m0} - \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta i_{sd} + \left( -\frac{k_{iqp} + R_s}{\sigma L_s} - \frac{R_r(1-\sigma)}{\sigma L_r} \right) \Delta i_{sq} + \left( -\frac{NL_m \omega_{m0}}{\sigma L_s L_r} \right) \Delta \psi_{rd} + \left( \frac{L_m R_r}{\sigma L_s L_r^2} \right) \Delta \psi_{rq} + \\ & \left( \frac{k_{iqi}}{\sigma L_s} \right) \Delta x_{sq} + \left( N\omega_{m0} + \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta i_{sd1}^* + \left( -\frac{R_r i_{sd0}^*}{L_r i_{sd20}^*} + \frac{(1-\sigma)R_r}{\sigma L_r} + \frac{R_r i_{sd10}^*}{L_r i_{sd20}^*} \right) \Delta i_{sq1}^* + \\ & \left( \frac{R_r i_{sd0}^* i_{sq10}^*}{L_r i_{sd20}^{*2}} - \frac{R_r i_{sd10}^* i_{sq10}^*}{L_r i_{sd20}^{*2}} + \left( \frac{(1-\sigma)N\omega_{m0}}{\sigma} \right) \right) \Delta i_{sd2}^* + \left( \frac{k_{iqp}}{\sigma L_s} \right) \Delta i_{sq}^* + \left( -N i_{sd0}^* + N i_{sd10}^* - \right. \\ & \left. \frac{NL_m \psi_{rd0}}{\sigma L_s L_r} + \frac{(1-\sigma)N i_{sd20}^*}{\sigma} \right) \Delta \omega_m \quad (Eq. 28) \end{aligned}$$

$$\frac{d}{dt} \Delta \psi_{rd} = \left( \frac{L_m R_r}{L_r} \right) \Delta i_{sd} + \left( -\frac{R_r}{L_r} \right) \Delta \psi_{rd} + \left( \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta \psi_{rq} + \left( \frac{R_r \psi_{rq0}}{L_r i_{sd20}^*} \right) \Delta i_{sq1} + \left( -\frac{R_r i_{sq10}^* \psi_{rq0}}{L_r i_{sd20}^{*2}} \right) \Delta i_{sd2}^* \quad (Eq. 29)$$

$$\frac{d}{dt} \Delta \psi_{rq} = \left( \frac{L_m R_r}{L_r} \right) \Delta i_{sq} + \left( \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta \psi_{rd} + \left( -\frac{R_r}{L_r} \right) \Delta \psi_{rq} + \left( -\frac{R_r \psi_{rq0}}{L_r i_{sd20}^*} \right) \Delta i_{sq1} + \left( \frac{R_r i_{sq10}^* \psi_{rd0}}{L_r i_{sd20}^{*2}} \right) \Delta i_{sd2}^* \quad (Eq. 30)$$

$$\frac{d}{dt} \Delta \omega_m = \left( -\frac{NL_m \psi_{rq0}}{J L_r} \right) \Delta i_{sd} + \left( \frac{NL_m \psi_{rd0}}{J L_r} \right) \Delta i_{sq} + \left( \frac{NL_m i_{sq0}^*}{J L_r} \right) \Delta \psi_{rd} + \left( -\frac{NL_m i_{sd0}^*}{J L_r} \right) \Delta \psi_{rq} + \left( -\frac{1}{J} \right) \Delta T_L \quad (Eq. 31)$$

$$\frac{d}{dt} \Delta x_{sd} = [-1] \Delta i_{sd} + \left( \frac{1}{2} \frac{L_s}{L_m^2} \left( \frac{2L_r(1+\sigma^2)i_{sq0}^*}{P} \right)^{-\frac{1}{2}} \right) \Delta i_{sq}^* \quad (Eq. 32)$$

$$\frac{d}{dt} \Delta x_{sq} = [-1] \Delta i_{sq} + [1] \Delta i_{sq}^* \quad (Eq. 33)$$

$$\frac{d}{dt} \Delta i_{sd1}^* = \left[ -\frac{1}{T_d} \right] \Delta i_{sd1}^* + \left[ \frac{1}{T_d} \right] \left( \frac{1}{2} \frac{L_s}{L_m^2} \left( \frac{2L_r(1+\sigma^2)i_{sq0}^*}{P} \right)^{-\frac{1}{2}} \right) \Delta i_{sq}^* \quad (Eq. 34)$$

$$\frac{d}{dt} \Delta i_{sq1}^* = \left[ -\frac{1}{T_d} \right] \Delta i_{sq1}^* + \left[ \frac{1}{T_d} \right] \Delta i_{sq}^* \quad (Eq. 35)$$

$$\frac{d}{dt} \Delta i_{sd2}^* = \left[ -\frac{1}{T_2} \right] \Delta i_{sd2}^* + \left[ \frac{1}{T_2} \right] \left( \frac{1}{2} \frac{L_s}{L_m^2} \left( \frac{2L_r(1+\sigma^2)i_{sq0}^*}{P} \right)^{-\frac{1}{2}} \right) \Delta i_{sq}^* \quad (Eq. 36)$$

With the equilibrium point as shown by  $\omega_{m0} = 209.4254$ ,  $i_{sd0}^* = 1$ ,  $i_{sq0}^* = 0.23914$

### 3 Results and Discussions

The induction motor used in this modeling uses an induction motor with specifications, namely a three-phase induction motor, 750 W, 1410 rpm, and 4 poles. The controller parameters used in the simulation process of each method are shown in Table 1-2. [15]

**Table 1.** Parameters of Induction Motor

Parameter	Symbol	Value
Pole pairs	P	2
Stator Resistance	$R_s$	2.76 $\Omega$
Rotor Resistance	$R_r$	2.9 $\Omega$
Stator Inductance	$L_s$	0.2349 H
Rotor Inductance	$L_r$	0.2349 H
Mutual Inductance	$L_m$	0.2279 H

**Table 2.** Controller Parameters

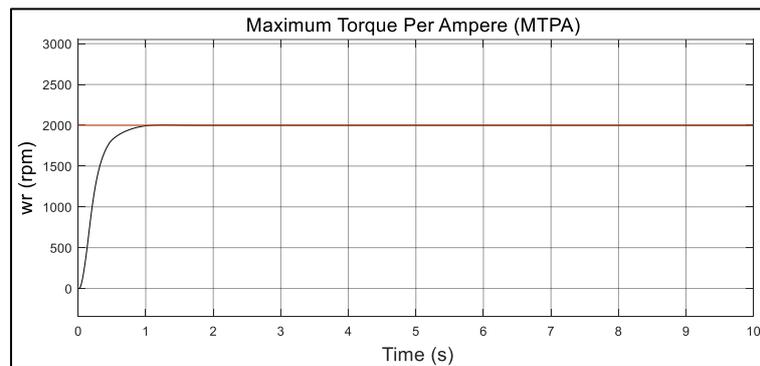
Parameter	Symbol	Value
Kp Speed Controller	Kp	0.9
Ki Speed Controller	Ki	0.2

Modeling test by providing several reference speed inputs at 2000 rpm, 2600 rpm, and 3000 rpm.

a. Testing with 2000 rpm speed reference

The induction motor with the type used with the maximum rate of 1410 rpm experiments increasing the speed by 2000 rpm. The response of the system is shown in Fig. 2. The rise time on system response is 390.146 ms. Overshoot of the response is 0.505%. In simulations the response of the system can follow its reference speed, there are overshoots and the time required to reach a steady state.

The output current for the flux controller current  $i_{sd}$  lagging slightly behind the reference current ( $i_{sd}^*$ ). Output of the system there is an immediate decrease towards the minimum current value. The response of  $i_{sd}$  current can follow its reference current ( $i_{sd}^*$ ) and  $i_{sq}$  decrease after the system reaches the reference current speed from the speed

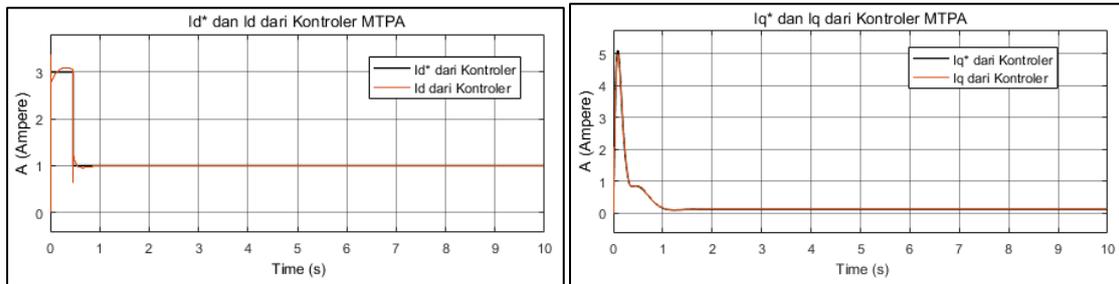
**Figure 2.** MTPA at 2000 rpm

controller ( $i_{sq}^*$ ). The system is a close loop system by getting error values as input for previous improvements. The response of the system is shown in Fig 3.

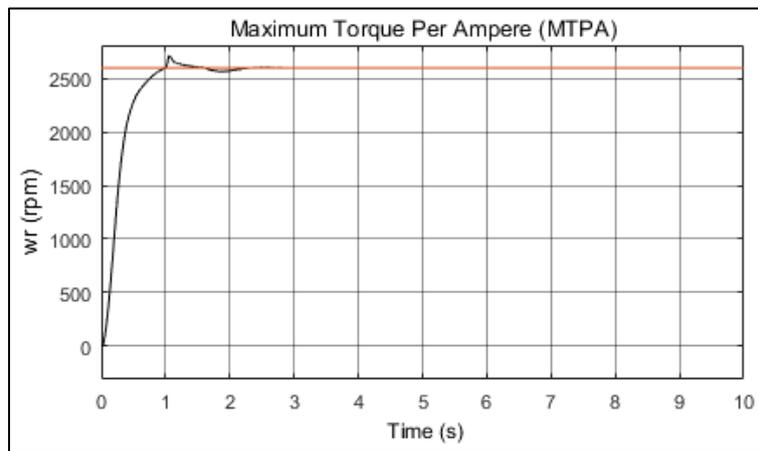
b. Testing with 2600 rpm speed reference

The test was carried out by providing a reference of 2600 rpm. The response of the system is shown in Fig 4. The rise time on system response is 442,739 ms. Overshoot of the response is 4.737%. From the overshoot value, the system is safe because the overshoot is still within the tolerance limit of 0 to 10%. The response of the system can follow its reference speed, in simulations, there are overshoots and several oscillations, and the time required to reach a steady state. However, the system can reach a steady-state state.

The current  $i_{sd}$  lags behind that of  $i_{sd}^*$ , and oscillations occur. The response from the  $i_{sd}$  follow the reference current ( $i_{sd}^*$ ) and can reach its steady state as shown in Fig. 5. The  $i_{sd}$  the current controller maintains with maximum current at 3A until the system reaches a speed of 2600 rpm. As for  $i_{sq}$  lagging compared to  $i_{sq}^*$ . The system follows the



**Figure 3.** Comparison  $i_{sq}^*$  with  $i_{sq}$  and  $i_{sd}^*$  with  $i_{sd}$  MTPA at 2000 rpm



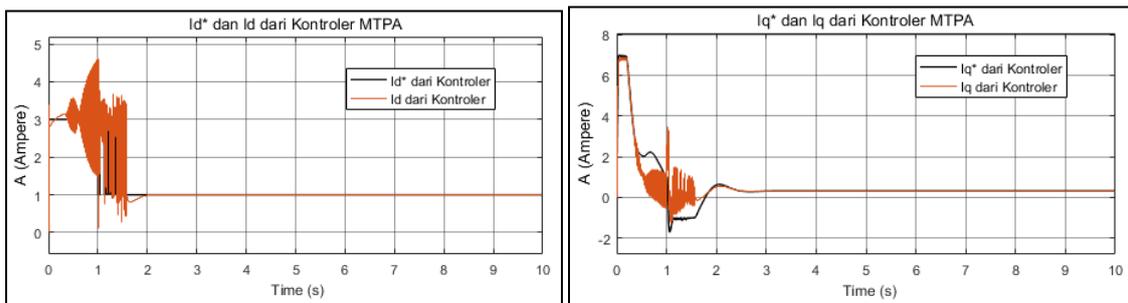
**Figure 4.** MTPA at 2600 rpm

references and reaches a steady-state state. The reference current undergoes oscillation and then reaches a steady-state state. The output value  $i_{sq}$  higher than the current in the previous condition. At a speed of 2600 rpm, the current controller is already at the limit of system saturation.

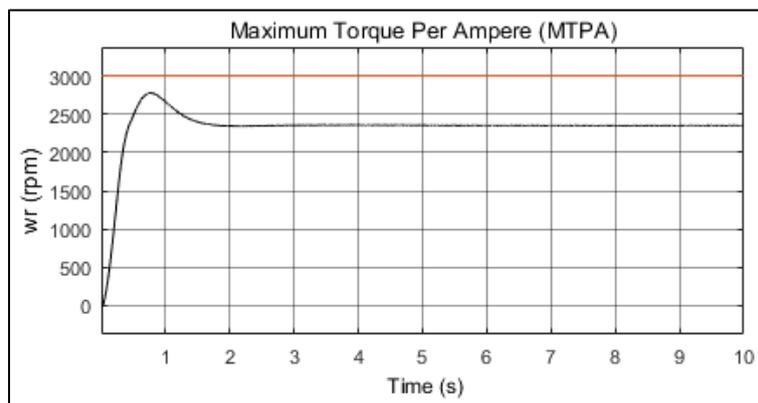
c. Testing with reference speed 3000 rpm.

The test was carried out by providing a reference of 3000 rpm. The response of the system cannot follow the reference speed, because the desired speed has exceeded the speed limit of the system. The system will only stay in the steady-state position even if it not reach its target speed. The response of the system is shown in Fig 6.

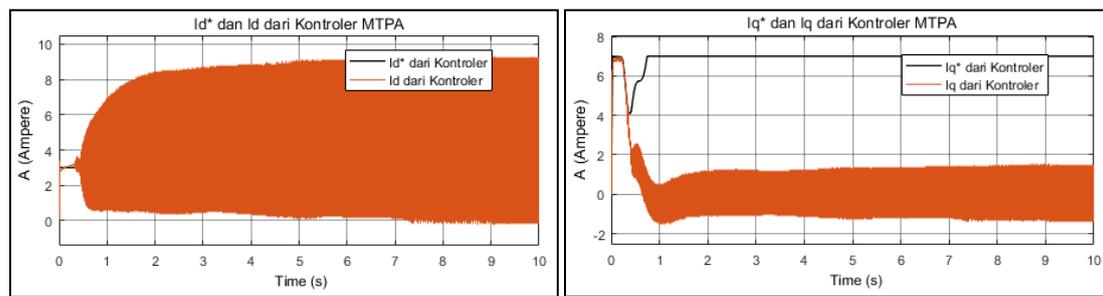
The current controller cannot maintain its current limit so the system failed to reach a steady-state state as shown in Fig. 7. The system continues to oscillate continuously because the system failed to reach the speed target. The desired speed exceeds the capabilities of the system so that the current from the  $i_{sd}$  still try to maintain the maximum current to reach its target speed. The condition of  $i_{sq}$  is also slightly behind



**Figure 5.** Comparison of  $i_{sq}^*$  with  $i_{sq}$  and  $i_{sd}^*$  with  $i_{sd}$  to MTPA  $i_{sd}$  at 2600rpm



**Figure 6.** MTPA at 3000 rpm



**Figure 7.** Comparison of  $i_{sd}^*$  to MTPA  $i_{sd}$  at 3000rpm

compared to  $i_{sq}^*$ . At first, the system followed the references, but the system failed to reach a steady-state state. The system failed to reach speed target and exceeded the system's capabilities so that the current from the  $i_{sq}$  will stop maintaining its maximum condition. The rate of the induction motor in this model is 1410 rpm. MTPA modeling can increase performance up to 2600 rpm. The modeling method with MTPA can increase performance by 84.4%

## 4 Conclusions

Studies on modeling with the Maximum Torque Per Ampere (MTPA) Method have been presented. The result of the modeling is that increasing the speed of each different reference input will affect settling time. The higher the speed, the longer it takes for the system to reach a steady-state state. The maximum speed that can be achieved is at a speed of 2600 rpm, so the MTPA method can increase the performance of three-phase induction motors by 84.4%. The above research is limited to the induction motor used is a squirrel cage type three-phase induction motor, and the system uses a speed sensor. The next research direction is to prove the stability of the system by analyzing pole position and movement with variations of  $K_p$ ,  $K_i$ , and  $K_d$  and combining the MTPA method with other methods to improve the performance of the induction motor.

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